

# Super Large Aperture Molecular Lasers

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**Abstract:** An excitation of super large aperture  $CO_2$ - and  $N_2O$ -lasers places demanding and unusual constraints on the pulsed power supply. Stable discharges with interelectrode gaps as large as g > 70 cm were achieved [1, 2] using pulsed power supplies [3] that satisfy specific requirements imposed by volume preionization and discharge ignition. The supply must initially apply a quasi-dc or slow-rise voltage to effect preliminary filling of the gap with electrons from an auxiliary discharge, followed by application of a controlled rise voltage to ignite a self-sustained volume discharge (SSVD). A coupled particle kinetics-equivalent circuit model has been developed to simulate discharge behavior for the various pulsed power configurations. Our computational results are compared with experiments involving super large aperture, huge volume devices [1-4].

### 1. VOLTAGE WAVEFORMS FOR SSVD INITIATION

### 1.1. Single-Pulse Waveforms

Three types of voltage waveforms have been used to establish SSVD in CO<sub>2</sub>-laser gas mixtures that are preionized by auxiliary discharges. As illustrated by the waveform shown in Fig. la, the first method uses a continuously increasing applied voltage (rise time  $t_r$ ) to sweep electrons generated by the auxiliary discharge across the main transverse gap and to ignite the discharge. The induced electron drift velocity is zero when the auxiliary discharge is initially fired and then increases as the voltage applied across the main gap  $U_d(t)$  rises. Preliminary filling should be complete before discharge ignition [5, 6], which requires that

$$t_{T} \ge (3/2)t_{dT} = \frac{9g^{2}}{4\mu e^{U} pk}.$$
(1)

Here  $t_{dr}$  is the characteristic drift time,  $\mu_e$  is the electron mobility, and  $U_{pk}$  is the peak discharge voltage.

The second method, as illustrated by the waveform in Fig. 1b, involves the application of a quasi-dc bias voltage  $U_{\text{bias}}$  for a duration which approximates or exceeds  $t_{dr}$ , i.e.,

$$t_{\text{bias}} \ge t_d r = \frac{g^2}{\mu_e U_{\text{bias}}}.$$
 (2)



**Figla-c.** Voltage waveforms for single-pulse excitation: (a) smoothly rising leading edge, (b) smoothly rising leading edge with preapplied quasi-dc bias, and (c) ramped bias voltage followed by smoothly rising leading edge [3].

The value chosen for the quasi-dc bias field,  $E_{\text{bias}} = U_{\text{bias}}/g$ , must be large enough to transport electrons across the gap in a reasonably short time but small enough to avoid operation in an E/Nregime where losses due to dissociative attachment are a problem. The preionization phase is followed by a gradually rising voltage to ignite the discharge. Sensible current begins to flow across the main gap at or just prior to the time of maximum applied voltage. The voltage rise time is again defined as t<sub>r</sub> and its value must be of sufficient duration to avoid premature depletion of the cathode space-charge layer during ignition; hence, there is a maximum rate of voltage rise,

$$\frac{dU_d}{dt}\Big|_{\max} = f(\text{gas composition}, P, J_{\text{aux}}),$$
(3)

that should not be exceeded. *P* is the total gas pressure, and  $J_{aux}$  is the current density produced by the auxiliary discharge for a duration  $t_{aux}$ . This method can lead to problems if the space-charge screen is suddenly depleted during commutation of the  $U_{bias}$  potential; this phenomenon occurs if the condition

$$E_{cf} \ll E_{\text{bias}}$$
 (4)

is violated, where  $E_{cf}$  is the field associated with the cathode fall. Condition (4) can be satisfied if  $U_{\text{bias}}$  is sufficiently small (which may not be practical) or if the auxiliary discharge is fired prior to commutation of  $U_{\text{bias}}$ .

The third method uses a slowly increasing ramp voltage waveform to transport the preionizing electrons across the interelectrode gap, followed by a more steeply increasing voltage to ignite the discharge (Fig. lc). The voltage initially increases from zero to  $U_{\text{ramp}}$  at  $t = t_{\text{ramp}}$  and then increases more abruptly to  $U_{pk}$  over a duration  $t_r$ . This method avoids those problems associated with sudden application of a quasi-dc bias at t = 0.

### **1.2. Double-Pulse Waveforms**

With this method, any of the three waveform types described previously in Sect. 1.1 is used to establish a low-current, quiescent SSVD. This plasma acts as a prepared load for discharge of a second, fast pulse power supply. The fast pulse circuit is optimized for maximum electrical efficiency.

### **1.3. Minimum Ignition Voltage**

A necessary but insufficient condition for discharge stability is

$$U_{pk} \ge \zeta U_{sb}, \tag{5}$$

where  $U_{sb}(E_{sb})$  is the self-breakdown voltage (field) for unprofiled electrodes.  $U_{sb}$  is roughly half the self breakdown value measured for profiled electrodes having a uniform electric-field distribution. The factor  $\zeta$  is stipulated differently depending upon the particular citation:  $\zeta = 1.8$ for g < 10 cm [7] and  $\zeta \sim 1.1$ -1.3 for g = 20-60 cm [3]. Operation with  $U_{pk} < \zeta U_{sb}$  causes arcs that occur shortly after the time of voltage maximum if the auxiliary discharge is on, and during the voltage rise if the auxiliary discharge is off or if  $t_{aux} < t_r$ .

## 2. COUPLED PARTICLE KINETICS EQUIVALENT CIRCUIT

The behavior of a pulse forming network (PFN) that provides the requisite voltage waveforms can be predicted by modeling the equivalent circuit shown in Fig. 2. The constitutive equations for circuit voltages and currents are

$$\frac{dU_1}{dt} = -\frac{I_1}{C_1},\tag{6}$$

$$\frac{dU_2}{dt} = -\frac{I_1 - I_2}{C_2},$$
(7)

$$\frac{dU_3}{dt} = -\frac{I_3}{C_3},\tag{8}$$

$$\frac{dI_1}{dt} = \frac{U_1 - R_1 I_1 - U_2}{L_1},$$
(9)

$$\frac{dI_2}{dt} = \frac{U_2 - R_2 I_2 - U_d}{L_2},$$
(10)

$$\frac{dI_3}{dt} = \frac{U_3 - R_3 I_3 - U_d}{L_3}.$$
(11)

The prolonged voltage rise necessary for dynamic profiling of the electric field is produced by the PFN which consists of capacitors  $C_1$  and  $C_2$  and inductors  $L_1$  and  $L_2$ .  $R_1$  and  $R_2$  represent resistive losses associated with the transmission lines and switchgear. Switch  $S_1$  is commuted at t = 0 which initiates discharge of energy-storage capacitor  $C_1$ . A second, fast rise-time voltage is superimposed upon the transverse gap at a later time by commuting switch  $S_2$  at  $t = t_f$ . This initiates discharge of energy-storage capacitor  $C_3$ .  $R_3$  represents resistive line and switch losses and resistor  $R_4$  is necessary to ensure reproducible switch closure and to partially reduce circuit ringing. These equations must be solved simultaneously with equations describing the electron, negative-ion, and  $N_2$ , metastable densities:

$$\frac{dn_{e}}{dt} = (\bar{k}_{i} - \bar{k}_{a})n_{e}N - k_{r}^{ei}n_{e}n_{+} + \bar{k}_{d}n_{-}N + \frac{n_{m}}{\tau_{p}},$$
(12)

$$\frac{dn_{-}}{dt} = \bar{k}_{a}n_{e}N - \bar{k}_{d}n_{-}N - k_{r}^{ii}n_{+}n_{-},$$
(13)

$$\frac{dn_m}{dt} = k_m n_e [N_2] - \frac{n_m}{\overline{\tau}},\tag{14}$$

where *n* represents particle concentration (particles/cm<sup>3</sup>) and the subscripts e, +, —, and m denote electrons, positive ions, negative ions, and metastable species, respectively. Processes (and rate coefficients) include primary electron-impact ionization  $(k_i)$ , electron attachment  $(k_a)$ , electron detachment  $(k_d)$ , electron-ion recombination  $({}^{k_r^{ei}})$ , ion-ion recombination  $({}^{k_r^{ii}})$ , and N<sub>2</sub> *a*-state excitation  $(k_m)$ . The bar notation indicates rate coefficients which are weighted for the particular gas mixture and which are functions of the local value of the reduced electric field *E/N*, where *N* is the total particle concentration. [N<sub>2</sub>] is the nitrogen gas concentration (constant).  $\overline{\tau}$  is the characteristic time for collisional deactivation of the metastable level (weighted for the particular gas mixture) and

 $\tau_p$  is the characteristic time for Penning collisions;  $1/\tau_p = k_p N_{ri}$ , where  $N_{ri}$  is the concentration of readily ionizable molecules such as tri-n-propylamine (TPA). The positive-ion density is found by assuming charge neutrality in the positive column:

$$n_{+} = n_{e} + n_{-}. \tag{15}$$



#### Fig2. Equivalent-circuit schematic diagram

The initial conditions for the system of ordinary differential equations (ODEs) are

$$U_1(0) = U_c,$$
 (16)

$$U_2(0) = U_d(0) = U_{\text{bias}},$$
(17)

$$U_3(0) = U'_c,$$
 (18)

$$I_1(0) = I_3(0) = I_d(0) = 0,$$
(19)

$$I_2(0) = U_{\text{bias}} / R_4,$$
 (20)

$$n_e(0) = n_{e0}, (21)$$

and

$$n_{-}(0) = n_{m}(0) = 0, \tag{22}$$

where  $U_e$  is the charging voltage on capacitor  $C_1$ ,  $U'_e$  is the charging voltage on capacitor  $C_3$ , and  $n_{e0}$  is the initial electron density.  $U_{\text{bias}}$  is the quasi-dc bias voltage applied to the gap prior to closure of either switch or  $S_2$ . If  $U_{\text{bias}} > 0$ , then a quasi-dc field was used to sweep preionizing electrons across the interelectrode gap and the initial potentials on capacitor  $C_2$  and the discharge gap are equal to  $U_{\text{bias}}$ . The duration of this preionization process ( $\sim t_{dr}$ ) does not enter into the present model since we assume that the entire interelectrode gap is uniformly filled with electrons with density  $n_{e0}$  at t = 0. The discharge voltage and current are

$$U_d(t) = \frac{I_2 R_4 R_d}{R_4 + R_d}$$
(23)

and

$$I_{d}(t) = I_{2} - \frac{U_{d}}{R_{4}}.$$
(24)

The discharge resistance is related to the electron density by

$$R_d(t) = \frac{g}{e\mu_e n_e A},\tag{25}$$

where e is the electronic charge and A is the effective discharge area. The contribution to plasma conductivity by positive- and negative-ion species is small and is neglected in (25). Because

 $\mu_e = \mu_e(E/N)$ , (25) must be solved iteratively and self-consistently along with (6-15). The bias voltage, if nonzero, is small enough that the discharge gap is initially non-conductive, i.e.,  $R_d(0) >> R_4$ . The instantaneous power supplied to the discharge is

$$P_d(t) = U_d(t)I_d(t), \tag{26}$$

the energy dissipated in the discharge is

$$E_d = \int P_d(t)dt,\tag{27}$$

the electrical efficiency is

$$\eta_{e1} = 2E_d / (C_1 U_e^2 + C_2 U_{\text{bias}}^2 + C_3 U_e'^2, \tag{28}$$

and the specific input energy is

$$\xi_i = E_d / V, \tag{29}$$

where *V* is the disharge volume.

With this model, we have the option of simulating either double-pulse excitation using the entire

circuit or single-pulse excitation using the reduced-form equivalent circuit (by setting  $t_f = \infty$ ). The system of differential equations was coded for computer solution using a robust ODE solver (LSODE from the Lawrence Livermore ODEPACK collection [8]). Rate and transport coefficients were determined separately by solution of the Boltzmann equation at tabulated values of E/N and then determined within the code using a fourth-order (cubic) Lagrangian interpolator [5].

### **3. PULSED POWER SYSTEMS**

Both Marx [3, 9] and Fitch-Howell [3, 10] pulse generators, with suitable modifications, have been used to produce the waveform types shown in Fig. 1. The equivalent circuit in the present model (Fig. 2) is applicable only to the former system. To produce the voltage waveform with a smoothly rising leading edge (Fig. la), the PFN parameters are adjusted so that

$$t_{\Gamma} \approx \pi \left(\frac{L_{\rm ICI}}{4}\right)^{1/2}.\tag{30}$$

where  $C_1 = C/N_s$  is the equivalent Marx bank capacitance, C is the capacitance of each stage, and  $N_s$  is the number of stages. The equivalent charging voltage is then  $U_c = N_s U_g$ , where  $U_g$  is the actual generator charging voltage. The approach in [3] typically use  $C_2 = C/N_s$ , so the discharge current period is

$$T \approx 2\pi (L_2 C_2)^{1/2}.$$
 (31)

The voltage waveform with a quasi-dc bias (Fig. lb) is produced simply by charging capacitor  $C_2$  to voltage  $U_{\text{bias}}$  and inserting the main switch between  $C_2$  and the discharge. No isolation switch is necessary between the Marx bank and  $C_2$  if  $U_{\text{bias}} = U_g$ . The voltage waveform with an initial ramp to  $U_{\text{ramp}}$  (Fig. lc) is produced by substituting a two-stage *LC* circuit for the single capacitor  $C_2$ .

### 4. COMPUTATIONAL RESULTS

### 4.1. Single-Pulse Excitation Without Quasi-dc Bias

The rise time  $t_r$  (cf. Fig. la) is adjusted by varying the ratio of PFN inductances, here expressed by the dimensionless parameter

$$M = \frac{L_1}{L_2}.$$
(32.33)

 $I_{pk}$  is the peak current which occurs at time  $t_{pk}$  and  $t_{qs}$  is defined by the full width at half maximum (FWHM) current pulse width. In this example, Q = 0.61,  $E_{qs} = 10$  kV/cm,  $I_{pk} = 13$  kA,  $t_{qs} = 0.8$   $\mu$  s,  $\eta_{e1} = 66\%$ , and  $\xi_i = 297$  J/l.



Fig3. Representative  $I_d - U_d$  waveforms for single-pulse excitation and definition of nomenclature.



Fig4. Computed and measured  $I_d - U_d$  waveforms for the device described in [11]

 $U_{\rm res}$  can be reduced by decreasing the parallel resistance  $R_4$ , but this occurs at the expense of reduced electrical efficiency. For example, the device in [11] employed a CO<sub>2</sub>:N<sub>2</sub>:He = 1:4:5 gas mixture at atmospheric pressure with g = 10 cm and A = 400 cm<sup>2</sup>. Stated circuit parameters were  $C_1 = 0.25 \,^{\mu}$  F,  $C_2 = 0.1 \,^{\mu}$  F,  $U_c = 120 \,\text{kV}$ ,  $L_1 \sim 15\text{-}20 \,^{\mu}$  H,  $L_2 \sim 1 \,^{\mu}$  H, and  $R_4 = 75/N_r \,^{\Omega}$ , where  $N_R$  is an unspecified number of resistors in parallel. The small value of  $R_4$  helps to prevent discharge voltage ringing and arc formation after the glow period. The choice of  $N_R$  strongly effects the computed value of  $I_{pk}$  and  $N_R = 2$  gave the best agreement with experiment. Assumed parameters were  $R_1=R_2 = 10 \,^{\text{m}}$  mQ,  $n_{e0} = 10^7 \,^{\text{cm}3}$ , and  $P_{ri} = 0.75 \,^{\text{Torr}}$  (TPA). Computations performed with these parameters gave values of  $t_r$  and  $t_{pk}$  which were too short, indicating that M was too small. By increasing to 35  $\,^{\mu}$  F (i.e., M = 35), voltage and current waveforms (Fig. 4) were obtained in approximate qualitative and quantitative agreement with measurements (the computations depicted in Figs. 3 and 4 are therefore identical with the exception of  $R_4$ ). The principal discrepancy is between the computed ( $t_{qs} = 0.9 \,^{\mu}$  s)

and experimental ( $t_{qs} = 1.4 \ \mu$  s) current pulse widths, which is probably related to two-dimensional effects such as the current density distribution across the electrodes. This circuit is poorly designed, viz.,  $\eta_{e1} = 34\%$  and  $\xi_i = 153$  J/l. The importance of Penning ionization of the readily ionizable additive is illustrated by a computational experiment with the N<sub>2</sub> metastable kinetics turned off. In this case,  $I_{pk} < 2$  kA.

It is useful to examine parametric regions where Q can be maintained below a specified minimum, i.e.,  $Q < Q_{\min}$ . For each value of  $Q_{\min}$  there exists an  $M_{\max} = M(Q_{\min})$  at which it is still possible to obtain  $Q < Q_{\min}$ . In the paper [9] found that  $M_{\max}$  is only weakly dependent upon  $L_1$ ,  $L_2$ ,  $C_1 = C_2$ , g, Aor  $n_{e0}$ . Concurrently, there exists a maximum value of  $t_r$  for each  $Q_{\min}$ ,  $t_{r,\max}$ , given by

$$t_{r,\max}(Q_{\min}) = \pi \left(\frac{L_2 C_1 M_{\max}}{4}\right)^{1/2}.$$
(34)

 $t_{r,max}$  can be increased by increasing inductance L<sub>2</sub>, but this also increases the discharge current pulse width. The duration of the SSVD can be crudely bounded by the duration of the discharge half-period [cf. (31)], i.e.,

$$t_{qs} \ge T_{1/2} = \pi (L_2 C_2)^{1/2}.$$
(35)

Combining (34) and (35) yields the condition

$$t_{r,\max} \le t_{qs} \left(\frac{M_{\max}}{4}\right)^{1/2}.$$
(36)

Thus, the maximum voltage rise time is limited by the requirement to deposit energy into the SSVD efficiently. The maximum permissible discharge gap can be estimated from the requirement for complete electron filling during the preionization phase as discussed previously, hence

$$g_{\max} \cong (0.3 - 0.4) \mu_e t_{r,\max} U_c / g, \tag{37}$$

where the numerical factor arises from the necessity to complete the preliminary filling process prior to discharge ignition. If we desire  $t_{qs} = 5^{\mu}$  s and  $Q_{min} = 0.3$ , then  $t_{r,max} \sim 15^{\mu}$  s. Using representative values of  $\mu_e = 10^3 \text{ cm}^2/\text{V-s}$  and  $U_c/g \sim 2U_{qs}/g = 10 \text{ kV/cm}$ , we obtain  $g_{max} = 40-50 \text{ cm}$  for atmospheric-pressure operation. The largest experimental values of g for this type of excitation are indeed comparable to this estimate [1-3]. Arc free SSVD in a 60-cm gap could only be obtained with a 50% probability by means of single-pulse excitation [1]. Note that (37) applies only for single pulse excitation without quasi-dc bias.

### 4.2. Single-Pulse Excitation With Quasi-dc Bias

In this type of excitation, the processes of preionization and discharge ignition are separate (cf. Fig. lb) and there is no maximum rise-time condition analogous to (34). Instead, there exists a maximum rate of voltage rise  $dU_d/dt/_{max}$  which produces consequential depletion of the negative space-charge layer covering the cathode. Operation with  $dU_d/dt > dU_d/dt/_{max}$  spoils the dynamic profiling process [cf. (3)] and reduces the probability for establishing a stable, homogeneous SSVD. For auxiliary barrier discharges,  $dU_d/dt/_{max} \sim 10 \text{ kV}/\mu \text{ s}$  [9]. By replacing the auxiliary barrier discharge with an auxiliary surface discharge, the maximum rate of voltage rise could be increased to  $dU_d/dt/_{max} \sim 30-40 \text{ kV}/\mu \text{ s}$  [2]. This attests to a higher productivity (larger  $J_{aux}$ ) by the surface discharge and allows a decrease in  $t_r$ .



**Fig5.** Computed dependence of the electrical efficiency  $\eta_{e1}$  on the voltage rise time  $t_r$ .



**Fig6.** Dependence of the dimensionless parameter Q on the voltage rise time  $t_r$ .

Table1. Computational parameters for single-pulse excitation with dc bias

Circuit parameters	Case (a)	Case (b)	Case (c)	
$C_1; C_2 [\mu F]$	0.25	0.50	0.15	
$L_1[\mu H]$	$ML_2$	$ML_2$	$ML_2$	
$L_2[\mu H]$	2.0	2.0	2.0	
$R_1;R_2[\Omega]$	0.01	0.01	0.01	
$R_4[\Omega]$	2000	2000	2000	
$U_{c}[kV]$	280	280	360	
U bias [kV]	56	56	72	
$E_s/V[J/1]$	200	400	200	
Geometry and initial conditions Gas mixture				
g[cm]	25	CO2: N2:He	1:4:5	
A[cm <sup>2</sup> ]	2000	Pri[Torr] (TPA)	0.75	
V[1]	50	P[Torr]	750	
Neo $[cm^{-3}]$	107	T [K]	293	

The current-voltage characteristics of a 50-1 device were numerically simulated to better understand the electrical design constraints that accompany this type of excitation. The parameters chosen for three cases are listed in Table 1 and would be typical of a 5-stage Marx bank. Case (a) is described by

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 $E_s/V \equiv \xi_i/\eta_{el} = 200$  J/l (i.e., ideal operation of this circuit would produce a specific input energy of 200 J/l) and by a peak discharge voltage which is above the ignition threshold but below the value for impedance matching. By varying  $L_1$  from 2 to 200  $^{\mu}$  H (M = 1 to 100),  $t_r$  can be adjusted over about

an order of magnitude. Computational results clearly show that although the discharge efficiency  $\eta_{e1}$  initially increases with increasing rise time (Fig. 5), circuit ringing is a persistent problem and no value of M produces Q < 0.3 (Fig. 6).  $t_{qs}$  increases gradually as a function of  $t_r$  and approaches the asymptote  $T_{1/2} = 2.2 \ ^{\mu}$  s.  $I_{pk}$  increases rapidly with  $t_p$  reaches a maximum at  $t_r \sim 3 \ ^{\mu}$  s ( $I_{pk} = 33$  kA), and then decreases gradually. The minimum degree of circuit ringing (Q = 0.34) and the maximum electrical efficiency ( $\eta_{e1} = 93\%$ ) occur simultaneously at  $t_r = 4 \ ^{\mu}$  s (M = 13). However, operation with such a short value of  $t_r$  yields a rate of voltage rise,  $dU_d/dt \sim (U_{pk} - U_{bias})/t_r = 40 \ \text{kV}/^{\mu}$  s, which is probably too large. If M and thus  $t_r$  are adjusted to reduce the maximum rate of voltage rise to  $dU_d/dt < 10 \ \text{kV}/^{\mu}$  s, then the large residual voltage amplitude (Q > 0.6) will invite arc formation at  $t = t_{res}$ .

Case (b) is identical to (a) with only a doubling in the capacitances  $C_1$  and  $C_2$  (i.e.,  $E_s/V \equiv \xi_i/\eta_{e1} = 400 \text{ J/l}$ , which may be above the maximum for this gas mixture and type of excitation). Since  $I_{pk} \propto (C_2/L_2)^{1/2}$  and  $t_{pk} \propto (C_1/L_1)^{1/2}$ , both parameters are characteristically larger in the present case, but discharge ringing is not alleviated. The minimum degree of circuit ringing (Q = 0.42) and the maximum electrical efficiency ( $\eta_{e1} = 89\%$ ) occur simultaneously at  $t_r = 5$   $\mu$  s (M = 13). Again, however, such a large rate of voltage rise ( $dU_d/dt \sim 30 \text{ kV}/\mu$  s) may preclude satisfactory operation at this value of  $t_p$ .

All of the energy stored in the PFN is deposited into the laser discharge in the first cycle of operation if their impedances are matched. Since the laser discharge is effectively a constant voltage load, this occurs only if

$$U_c \cong 2U_{qs}.$$
(38)

Case (c) maintains  $E_s/V \equiv \xi_i/\eta_{e1} = 200 \text{ J/1}$  as in case (a) but increases the charging voltage to  $U_c = 360 \text{ kV}$  in conformance with this condition. C<sub>1</sub> and C<sub>2</sub> are decreased accordingly. Optimization of the circuit is now possible with marked improvement in current-voltage characteristics. Minimum circuit

ringing (Q = 0.28) and maximum electrical efficiency ( $\eta_{e1} = 98\%$ ) occur concurrently at  $t_r = 2.0 \ \mu$  s. The glow duration ( $t_{qs} = 1.3 \ \mu$  s) is now approximately the same as in the previous cases and the peak current ( $I_{pk} = 44$  kA) is approximately equal to the maximum encountered with case (b). Note that a value of  $Q \sim 0$  is not obtained because (38) is valid only if  $C_1 = C_2$  and  $U_{\text{bias}} = 0$ . While the optimization described here appears to adjacent to the cathode is not depleted. After establishment of the quiescent SSVD, additional energy can be rapidly loaded without disruption of plasma homogeneity or stability [1, 2].

To achieve a deliberately prolonged rise time for practical devices, however, it is often necessary to increase *M* to a value for which impedance matching between the PFN and load is poor. Typically, the PFN impedance is larger than the load (laser discharge) and the voltage waveform oscillates as shown by the example in Fig. 3. This computation was performed for a small (g = 10 cm,  $A = 400 \text{ cm}^2$ ), atmospheric-pressure (CO<sub>2</sub>:N<sub>2</sub>:He = 1:4:5) device with electrical parameters  $C_1 = 0.25 \ \mu$  F,  $C_2 = 0.1 \ \mu$  F,  $U_c = 120 \text{ kV}$ ,  $L_1 = 35 \ \mu$  H,  $L_2 = 1 \ \mu$  H,  $R_1 = R_2 = 10 \ m\Omega$ ,  $R_4 = 2 \ k\Omega$ ; also,  $n_{e0} = 10 \ \text{cm}^{-3}$  and  $P_{ri} = 0.75 \ \text{Torr}$  (TPA). If  $U_{res}$  is defined as the amplitude of the second or *residual* voltage peak which occurs at time  $t_{res}$  and if  $U_{qs}$  is defined as the discharge voltage at peak discharge current, then it is useful to find the electrical circuit parameters which minimize the dimensionless parameter

$$Q = \frac{U_{\rm res}}{U_{\rm qs}}.$$



**Fig7.** Computed  $I_d$ — $U_d$  waveforms for double-pulse excitation of the device described in [1]

Waveforms for single- and double pulse excitation of a 60-cm aperture, 120-1 device are given in [1]. The atmospheric-pressure gas mixture (CO<sub>2</sub>:N<sub>2</sub>:He = 4:16:80) was preionized by an auxiliary barrier discharge attached to the top surface of the cathode. Explicit PFN parameters are not given. For the double-pulse computation, therefore, numerical simulations were performed to find electrical parameters which would produce a quiescent plasma having an electron concentration  $n_e \sim 10^{10}$  cm<sup>-3</sup> at the conclusion of a slowly rising voltage pulse of duration

$$t_r \approx \frac{9g^2}{4\mu_e U_e (C_1/C_2)^{1/2}}.$$
(39)

Then at  $t_f = t_r$ , switch  $S_2$  is closed, depositing ~ 200 J/l into the plasma in accordance with impedancematching condition 138). To yield these results, a double-pulse PFN was designed with electrical parameters  $C_1 = 0.2 \ \mu$  F,  $C_2 = 0.1 \ \mu$  F,  $C_3 = 0.2 \ \mu$  F,  $L_1 = 1200 \ \mu$  H,  $L_2 = 100 \ \mu$  H,  $L_3 = 5 \ \mu$  H,  $R_1$ =  $R_2 = R_3 = 10 \ m\Omega$ ,  $R_4 = 5 \ k\Omega$ ,  $U_c = 180 \ kV$ ,  $U_{bias} = 45 \ kV$ ,  $U'_c = 520 \ kV$ ; also,  $n_{e0} = 5 \times 10^6 \ cm^{-3}$  and  $P_{ri} = 1.5 \ Torr$ . Closure of switch  $S_1$  produces a gradual increase in  $U_d$  to 220 kV over a duration  $t_r = 30 \ \mu$  s, generating a current flow of only  $I_d \sim 10$  A. Note that this PFN is designed as a voltage multiplier (i.e.,  $C_1 > C_2$ ) so that  $U_d(t_r) > \zeta U_{sb}$  even though  $U_c < \zeta U_{sb}$ . The PFN that consists of capacitors  $C_1$  and  $C_2$  and inductors  $L_1$  and  $L_2$  is effectively isolated from the second discharge pulse produced by the  $L_3 - C_3$  PFN provided that  $L_2 >> L_3$ . Furthermore, the stored energy for the first pulse is only 12% of that for the second, main pulse. Computed  $I_d - U_d$  waveforms for the time interval encompassing the second pulse are shown in Fig. 7.

**Table2.** Comparison of computed and experimental discharge parameters for double-pulse excitation of a 120-1 device

Parameter	Experiment [1]	Computation
tr [µS]	≈ 30-45	30
U d(tr) [kV]	240	221
ne (tr) [cm -3]		9x1010
Upk [kV]	≈ 380	393
U qs [kV]	≈ 290	355
tqs [µS]	≈ 3	2.1
Ipk [kA]	42	32.1
ζi [J/1]	<u>~</u> 180	188
$\eta_{eI}$	~ 0.90	0.74

Measured and computed discharge parameters are listed in Table 2. This type of excitation produces a shorter-duration, higher-current SSVD than possible with single-pulse excitation in qualitative agreement with experiment. The computed values of  $U_{qs}$  and  $I_{pk}$  are respectively larger and smaller

than the experimental measurements, but the agreement between  $\xi_i$  values is excellent. Furthermore, it is now possible to vary  $t_{qs}$  and therefore  $I_{pk}$  by adjusting  $L_3$  without sacrificing electrical efficiency. The simulation here showed little circuit oscillation beyond the first cycle (i.e., Q < 0.1).

A 140-1 device with a 70-cm interelectrode gap is described in [2]. This device employed an auxiliary surface discharge that was placed beneath the mesh cathode. The cathode was operated at ground potential and the auxiliary discharge was fed by a separate pulsed- power system. Electrons were repelled from the surface-discharge plasma and through the grid by applying a negative bias voltage to the auxiliary-discharge circuit. VUV radiation is only produced during the breakdown process for this type of auxiliary discharge whereas electrons can be extracted during the entire duration  $t_{aux}$ . PFN parameters are not given and the  $I_d - U_d$  waveforms are described as being qualitatively similar to those in [1]. For the present simulation, PFN parameters that initially establish a quiescent SSVD were again chosen by trial and error. The second, high-current discharge then operates according to impedance matching condition (38). The interelectrode gap is filled both by an initial burst of photoelectrons produced by surface-discharge VUV radiation and from electrons extracted from the

surface-discharge plasma during the entire quiescent period. The computed specific input energy ( $\xi_i$ 

= 130 J/l) is in good agreement with experiment ( $\xi_i = 140$  J/l) and the computed electrical efficiency is quite have alleviated the impedance matching problem, the large rate of voltage rise ( $dU_d/dt \sim 100$  kV/ $\mu$ s) will certainly destroy the cathode space-charge screen for even the highest productivity auxiliary discharges. Establishment of a stable SSVD under these conditions is highly unlikely.

## 4.3. Double-Pulse Excitation

This type of excitation is produced by firing the left-hand PFN (switch  $S_1$ ) at decreased charging voltage and stored energy, which produces a slowly increasing discharge voltage waveform and establishes a low-current but stable SSVD, followed by commutation of switch  $S_2$ , which dumps the main energy store (capacitor  $C_3$  charged to voltage  $U'_c$ ) into the plasma. The advantage here is that

the SSVD is established under *low-*  $dU_d/dt$  conditions and the negative space-charge layer high ( $\eta_{e1} = 80\%$ ).

## 5. CONCLUSIONS

Computational runs using a coupled particle kinetics equivalent circuit model were performed to simulate response of the various PFNs that are used with the auxiliary discharge excitation scheme. A single pulse PFN, with or without quasi-dc bias, can only be employed with g < 40-50 cm, in excellent agreement with experimental findings. This limitation is imposed by design conflicts between the need for increasingly longer rise times as the gap is increased and the requirement for impedance matching between the PFN and discharge plasma load. Larger discharge gaps require more complex circuitry to first establish a low-current, quiescent SSVD using a slow rise time initial pulse, followed by a second high current, fast rise time pulse that deposits the bulk of the stored energy into the discharge plasma of super large aperture molecular lasers [12-14].

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